# Neural Symbolic Language Understanding

Ni Lao 11.12.2017

Everything presented here is publicly available. The opinions stated here are my own, not those of Google.

### Plan

#### • Language & control

- Neural Symbolic Machines: Semantic Parsing on Freebase with Weak Supervision
  - Chen Liang, Jonathan Berant, Quoc Le, Kenneth Forbus, Ni Lao
- Knowledge & scalability
  - Learning to Organize Knowledge with An *N-Gram Machine* 
    - Fan Yang, Jiazhong Nie, William Cohen, Ni Lao

# Language & Reasoning

- Language was primarily invented for reasoning
- Communication comes later

### WHY ONLY US LANGUAGE AND EVOLUTION



Robert C. Berwick - Noam Chomsky



LOGIC AND MATHEMATICS ARE NOTHING BUT SPECIALISED LINGUISTIC STRUCTURES.

### ACL [Liang+ 2017] Language, Translation & Control

- 1) Natural languages are programming languages to control human behavior
- For machines and human to understand each other, they just need translation models trained with control theory

#### [Berant+ 2013] [Liang 2013]

### **Semantic Parsing**

- Question answering with structured data (KG / tables / personal data)
- Voice to action
- Personal assistant
- Entertainment



### **Question Answering with Knowledge Base**



### WebQuestionsSP Dataset

- 5,810 questions Google Suggest API & Amazon MTurk<sup>1</sup>
- Remove invalid QA pairs<sup>2</sup>
- 3,098 training examples, 1,639 testing examples remaining
- Open-domain, and contains grammatical error
- Multiple entities as answer => macro-averaged F1

**Grammatical error** 

**Multiple entities** 

- What do Michelle Obama do for a living?
- What character did Natalie Portman play in Star Wars?
- What currency do you use in Costa Rica?
- What did Obama study in school?
- What killed Sammy Davis Jr?

writer, lawyer Padme Amidala Costa Rican colon political science throat cancer

### (Scalable) Neural Program Induction

• Impressive works to show NN can learn addition and sorting, but...



Output



RESET

observation

• The learned operations are not as scalable and precise.



 Why not use existing modules that are scalable, precise and interpretable?





I'm Feeling Lucky

Google Search

### **Neural Symbolic Machines**



### Contributions

• Simple Seq2Seq model is not enough

#### 1. Compositionality



1. Key-Variable Memory

2. Beam search + Code Assistance

2. Large Search Space

E.g., Freebase:

23K predicates,

82M entities,

417M triplets

#### 3. Optimization

Reinforcement Learning is known to be hard given sparse reward



**3. Augmented REINFORCE** 

### **Key-Variable Memory for Compositionality**



• A linearised bottom-up derivation of the recursive program



### **Key-Variable Memory: Save Intermediate Value**



### **Key-Variable Memory: Reuse Intermediate Value**



#### **Code Assistance: Prune Search Space**



Pen and paper

#### **Code Assistance: Syntactic Constraint**



Decoder Vocab

### **Code Assistance: Syntactic Constraint**



Decoder Vocab

#### **Code Assistance: Semantic Constraint**



### **Code Assistance: Semantic Constraint**



# Policy Gradient (REINFORCE)

• MLE optimizes log likelihood of approximate gold programs

 $J^{ML}(\theta) = \sum \log P(a_{0:T}^{best}(q)|q,\theta)$ 

• **RL** optimizes the expected reward under a stochastic policy P

$$J^{RL}(\theta) = \sum \mathbb{E}_{P(a_{0:T}|q,\theta)}[R(q, a_{0:T})]$$



• The gradient is almost the same as that for MLE except for a weight P(R-B)

$$\nabla_{\theta} J^{RL}(\theta) = \sum_{q} \sum_{a_{0:T}} \left[ P(a_{0:T} | q, \theta) [R(q, a_{0:T}) - B(q)] \nabla_{\theta} \log P(a_{0:T} | q, \theta) \right]$$

• The baseline does not change the solution but improves convergences, e.g.,

$$B(q) = \sum_{a_{0:T}} P(a_{0:T}|q,\theta) R(q,a_{0:T})$$

[Williams 1992]

#### **REINFORCE** Training



#### Iterative Maximum Likelihood Training (Hard EM)



$$J^{ML}(\theta) = \sum_{q} \log P(a_{0:T}^{best}(q)|q,\theta)$$

#### Augmented REINFORCE



stabilize training

#### **Distributed Architecture**

• 200 actors, 100 KG servers, 1 learner



#### New State-of-the-Art on *WebQuestionsSP*

- First end-to-end neural network to achieve SOTA on semantic parsing with weak supervision over large knowledge base
- The performance is approaching SOTA with full supervision

Model	Avg. Prec.@1	Avg. Rec.@1	Avg. F1@1	Acc.@1
STAGG	67.3	73.1	66.8	58.8
NSM – our model	70.8	76.0	69.0	59.5
STAGG (full supervision)	70.9	80.3	71.7	63.9

#### Augmented REINFORCE

- REINFORCE get stuck at local maxima
- Iterative ML training is not directly optimizing the F1 score
- Augmented REINFORCE obtains the best performances

Settings	Train Avg. F1@1	Valid Avg. F1@1
iterative ML only	68.6	60.1
<b>REINFORCE</b> only	55.1	47.8
Augmented REINFORCE	83.0	67.2

### Plan

- Language & control
  - *Neural Symbolic Machines*: Semantic Parsing on Freebase with Weak Supervision
    - Chen Liang, Jonathan Berant, Quoc Le, Kenneth Forbus, Ni Lao

#### • Knowledge & scalability

- Learning to Organize Knowledge with An *N-Gram Machine* 
  - Fan Yang, Jiazhong Nie, William Cohen, Ni Lao

[Wickman 2012] [Bartol+ 2015]

# Where does knowledge come from?

- The human brain contains roughly 100 billion neurons each capable of making around 1,000 connections
- Where do we get these 100 TB parameters?
- How many lines of code do I need to write if I want to achieve AI?



## The Mind's Eye

PROBABLY APPROXIMATELY CORRECT Nature's Algorithms for Learning and Prospering in a Complex World



the world

a small machine which can copy large amount of complexity from the world to the brain

a suitable representation

[Vannevar Bush 1945]

# Knowledge and Scalability

 How information should be organized for scalability?

### **"AS WE MAY THINK"** (1945)



Consider a future device for individual use, which is a sort of mechanized private file and library. It needs a name, and to coin one at random, memex will do. A memex is a device in which an individual stores all his books, records, and communications, and which is mechanized so that it may be consulted with exceeding speed and flexibility. It is an enlarged intimate supplement to his memory.

# Scalability of modern search engines

- Can respond to user's requests within a fraction of a second
- But are weak at text understanding and complex reasoning



# Scalability of mammal memory



- Very rapid adaptation (in just one or a few trials) is necessary for survival
  - $\circ$   $\,$  E.g., associating taste of food and sickness  $\,$
- Need fast responses based on large amount of knowledge
  - Needs good representation of knowledge
- However, good representation can only be learnt gradually
  - During sleeps
  - to prevent interference with established associations

[Garcia+ 1966] [Wickman 2012] [Bartol+ 2015]

## **Complementary Learning Theory**

[McClelland+ 1995] [Kumaran+ 2016]



### (Scalable) Neural Nets

• Impressive works to show NN can learn addition and sorting, but...



NPI state

Environmen

observation

Next

Input program

RESET

NPI state

• The learned operations are not as scalable and precise.



• Why not use existing modules that are scalable, precise and interpretable?





Google Search

[Zaremba & Sutskever 2016]

I'm Feeling Lucky

## Question answering as a simple test bed



#### [Weston+ 2015]

## Facebook bAbl Tasks

- Simulated question answering tasks to test the ability to "**understand**"
- We introduce a special version ("life-long bAbl"), which has stories of up to 10 million sentences

Sam walks into the kitchen.	Brian is a lion.	Mary journeyed to the den.
Sam picks up an apple.	Julius is a lion.	Mary went back to the kitchen.
Sam walks into the bedroom.	Julius is white.	John journeyed to the bedroom.
Sam drops the apple.	Bernhard is green.	Mary discarded the milk.
Q: Where is the apple?	Q: What color is Brian?	Q: Where was the milk before the den?
A. Bedroom	A. White	A. Hallway

## The Knowledge Storage

- Each tuple in the KG is an n-gram, which is a list of symbols
- Each tuple is also associated with a timestamp to reason over time

Table 1: Example of probabilistic knowledge storage. Each sentence may be converted to a distribution over multiple tuples, but only the one with the highest probability is shown here.

Sentences	Knowledge tuples		
	Time stamp	Symbols	Probability
Mary went to the kitchen.	1	mary to kitchen	0.9
Mary picked up the milk.	2	mary the milk	0.4
John went to the bedroom.	3	john to bedroom	0.7
Mary journeyed to the garden.	4	mary to garden	0.8

## The Programs

• A **program** *C* is a list of **expressions**  $c_1...c_N$ , where each  $c_i$  is either a special expression *Return* indicating the end of the program, or is of the form (*F*,  $A_1...A_L$ )

Table 2: Functions in N-Gram Machines. The knowledge storage on which the programs can execute is  $\Gamma$ , and a knowledge tuple  $\Gamma_i$  is represented as  $(i, (\gamma_1, \ldots, \gamma_N))$ . "FR" means *from right*.

Name	Inputs	Return
Нор	$v_1 \dots v_L$	$\{\gamma_{L+1} \mid \text{ if } (\gamma_1 \dots \gamma_L) == (v_1, \dots, v_L), \forall \Gamma \in \mathbf{\Gamma} \}$
HopFR	$v_1 \dots v_L$	$\{\gamma_{N-L} \mid \text{ if } (\gamma_{N-L+1} \dots \gamma_N) == (v_L, \dots, v_1), \forall \Gamma \in \mathbf{\Gamma} \}$
Argmax	$v_1 \dots v_L$	$\operatorname{argmax}_{i}\{(\gamma_{L+1}, i) \mid \text{ if } (\gamma_{1} \dots \gamma_{L}) == (v_{1}, \dots, v_{L}), \forall \Gamma_{i} \in \mathbf{\Gamma}\}$
ArgmaxFR	$v_1 \dots v_L$	$\operatorname{argmax}_{i}\{(\gamma_{N-L}, i) \mid \text{ if } (\gamma_{N-L+1} \dots \gamma_{N}) == (v_{L}, \dots, v_{1}), \forall \Gamma_{i} \in \mathbf{\Gamma}\}$

# Example KS & Program

Table 6: Task 2 Two Supporting Facts

Story	Knowledge Storage
Sandra journeyed to the hallway. John journeyed to the bathroom. Sandra grabbed the football. Daniel travelled to the bedroom. John got the milk. John dropped the milk.	Sandra journeyed hallway John journeyed bathroom Sandra got football Daniel journeyed bedroom John got milk John got milk
Question	Program
Where is the milk?	ArgmaxFR milk got Argmax V1 journeyed

#### CopyNet [Gu+ 2016] NSM [Liang+ 2017]

## Seq2Seq components

- A **knowledge encoder** that converts sentences to knowledge tuples and defines a distribution  $P(\Gamma_i | s_i, s_{i-1}; \theta_{enc})$  s<sub>i-1</sub> for co-references
  - The probability of a KS  $\Gamma = \{\Gamma_1 \dots \Gamma_n\}$  is the product of its tuples' probabilities:

$$P(\mathbf{\Gamma}|\mathbf{s};\theta_{\text{enc}}) = \Pi_{\Gamma_i \in \mathbf{\Gamma}} P(\Gamma_i|s_i, s_{i-1};\theta_{\text{enc}})$$

• A **knowledge decoder** that converts tuples back to sentences and defines a distribution  $P(s_i|\Gamma_i, s_{i-1}; \theta_{dec})$  -- it will enable unsupervised training

• A **programmer** that converts questions to programs and defines a distribution  $P(C|q, \Gamma; \theta_{prog})$   $\Gamma$  for code assist

## Inference

Given an example (s, q, a) from our training set, we would like to maximize the expected reward

$$O^{QA}(\theta_{\rm enc}, \theta_{\rm prog}) = \sum_{\mathbf{\Gamma}} \sum_{C} P(\mathbf{\Gamma} | \mathbf{s}; \theta_{\rm enc}) P(C | q, \mathbf{\Gamma}; \theta_{\rm prog}) R(\mathbf{\Gamma}, C, a),$$

For gradient estimations we apply **beam search** instead of **MCMC**, which has huge variances

It leads to a **hard search problem**, which we solve by having 1) a stabilized **auto-encoding** objective to bias the encoder to more interesting hypotheses;

$$O^{AE}(\theta_{enc}, \theta_{dec}) = \mathbb{E}_{p(z|x;\theta_{enc})} [\log p(x|z;\theta_{dec})] + \sum_{z \in \mathbf{Z}^{N}(x)} \frac{\log p(x|z;\theta_{dec})}{\left[ \frac{\mathbb{Z}^{N}(x): \text{ all tuples of length N which only consist of words from x} \right]}$$

2) a **structural tweak** procedure which retrospectively corrects the inconsistency among multiple hypotheses so that reward can be achieved

 While code assist uses the knowledge storage to inform the programmer, structure tweak adjusts the knowledge encoder to cooperate with an uninformed programmer.



### Optimization

• For training stability and tweaking, we augment the training objective with **experience replays** 

$$\nabla_{\theta_{dec}} O'(\theta) = \sum_{s_i \in \mathbf{s}} \sum_{\Gamma_i} [\beta(\Gamma_i) + P(\Gamma_i | s_i, s_{i-1}; \theta_{enc})] \nabla_{\theta_{dec}} \log P(s_i | \Gamma, s_{i-1}; \theta_{dec}),$$

$$\beta(\Gamma_i) \text{ is 1 if } \Gamma_i \text{ only contains tokens from } s_i \text{ and 0 otherwise}$$

$$\nabla_{\theta_{enc}} O'(\theta) = \sum_{s_i \in \mathbf{s}} \sum_{\Gamma_i} [P(\Gamma_i | s_i, s_{i-1}; \theta_{enc}) \log P(s_i | \Gamma_i, s_{i-1}; \theta_{dec}) + \mathcal{R}(\mathcal{G}'(\Gamma_i)) + \mathcal{R}(\mathcal{G}(\Gamma_i))] \nabla_{\theta_{enc}} \log P(\Gamma_i | s_i, s_{i-1}; \theta_{enc}),$$
where  $\mathcal{R}(\mathcal{G}) = \sum_{\Gamma \in \mathcal{G}} \sum_{C} P(\Gamma | \mathbf{s}; \theta_{enc}) P(C | q, \Gamma; \theta_{prog}) R(\Gamma, C, a)$  is the total expected reward for

a set of valid knowledge stores  $\mathcal{G}, \mathcal{G}(\Gamma_i)$  is the set of knowledge stores which contains the tuple  $\Gamma_i$ , and  $\mathcal{G}'(\Gamma_i)$  is the set of knowledge stores which contains the tuple  $\Gamma_i$  through tweaking.

$$\nabla_{\theta_{\text{prog}}} O'(\theta) = \sum_{\Gamma} \sum_{C} \left[ \alpha I \left[ C \in \mathcal{C}^*(\mathbf{s}, q) \right] + P(C|q, \Gamma; \theta_{\text{prog}}) \right] \cdot P(\Gamma|\mathbf{s}; \theta_{\text{enc}}) R(\Gamma, C, a) \nabla_{\theta_{\text{prog}}} \log P(C|q, \Gamma; \theta_{\text{prog}}),$$
where  $\mathcal{C}^*(\mathbf{s}, q)$  is the experience replay buffer for  $(\mathbf{s}, q)$ .  $\alpha = 0.1$  is a constant. During training, the program with the highest weighted reward (i.e.  $P(\Gamma|\mathbf{s}; \theta_{\text{enc}}) R(\Gamma, C, a)$ ) is added to the replay buffer.

• optimize by **coordinate ascent** – updating three components in alternation with **REINFORCE** 

## Learning to search



### Results

• The bAbI dataset contains twenty tasks in total. We consider the subset of them that are extractive question answering tasks

Table 3: Test accuracy on bAbI tasks with auto-encoding (AE) and structure tweak (ST)

	Task 1	Task 2	Task 11	Task 15	Task 16
MemN2N	1.000	0.830	0.840	1.000	0.440
QA	0.007	0.027	0.000	0.000	0.098
QA + AE	0.709	0.551	1.000	0.246	1.000
QA + AE + ST	1.000	0.853	1.000	1.000	1.000

## Results

- AE is a strong bias towards good representations
- ST helps to achieve consistency, e.g.,
  - "he" vs "john" (coreference)
  - "cat" vs "cats" (singular vs. plural)
  - "go to" vs "journey to" (synonyms)

QA	QA + AE	QA + AE + ST
went went went	daniel went office	daniel went office
mary mary mary	mary <u>back</u> garden	mary <u>went</u> garden
john john john	john <u>back</u> kitchen	john <u>went</u> kitchen
mary mary mary	mary <u>grabbed</u> football	mary <u>got</u> football
there there there	sandra got apple	sandra got apple
cats cats cats	<u>cats</u> afraid wolves	<u>cat</u> afraid wolves
mice mice mice	<u>mice</u> afraid wolves	<u>mouse</u> afraid wolves
is is cat	gertrude is cat	gertrude is cat

## Result

• Scalability



### Thanks!

#### **Generated Programs**

- Question: "what college did russell wilson go to?"
- Generated program:

```
(hop v1 /people/person/education)
(hop v2 /education/education/institution)
(filter v3 v0 /common/topic/notable_types )
<EOP>
```

In which

• Distribution of the length of generated programs

#Expressions	0	1	2	3
Percentage	0.4%	62.9%	29.8%	6.9%
<i>F1</i>	0.0	73.5	59.9	70.3

### Mandelbrot Set





$$c \in M \iff \lim_{n \to \infty} |z_{n+1}| \le 2$$
 49

## Structure Tweak

- No reward
  - Caused by semantic (i.e. run-time) errors
    - Program: Hop var *cats*
    - Knowledge tuple: *Cat* afraid wolves
  - Propose knowledge tuples that allow the program with high probability to obtain positive reward
- Low expected reward
  - program with high reward in  $P(prog|q, kg) \neq program with high probability in <math>P(prog|q)$ 
    - "Hop var *journeyed*" vs "Hop var *went*"
  - Propose knowledge tuples that allow program with high probability to obtain high rewards

# Example KS & Program

Table 8: Task 15 Basic Deduction

Story	Knowledge Storage
Sheep are afraid of cats. Cats are afraid of wolves. Jessica is a sheep. Mice are afraid of sheep. Wolves are afraid of mice. Emily is a sheep. Winona is a wolf. Gertrude is a mouse.	Sheep afraid cats Cat afraid wolves Jessica is sheep Mouse afraid sheep Wolf afraid mice Emily is sheep Winona is wolf Gertrude is mouse
Question	Program
What is Emily afraid of?	Hop Emily is Hop V1 afraid

## Example KS & Program

Table 9: Task 16 Basic Induction

Story	Knowledge Storage
Berhard is a rhino. Lily is a swan. Julius is a swan. Lily is white. Greg is a rhino. Julius is white. Brian is a lion. Bernhard is gray. Brian is yellow.	Bernhard a rhino Lily a swan Julius a swan Lily is white Greg a rhino Julius is white Brian a lion Bernhard is gray Brian is yellow
Question	Program
What color is Greg?	Hop Greg a HopFR V1 a Hop V2 is